UNIVERSITY OF JAFFNA, SRI LANKA FACULTY OF ALLIED HEALTH SCIENCES Second Year First Semester Examination in B.Pharm Hons-2021 PHAMM 2111-PHARMACEUTICAL MATHEMATICS

Date: 01.02.2023

Time: One hour

Answer All Questions

1. (a) i. Examine the nature of roots in each of the following quadratic equations and also verify them by quadratic formula.

•
$$x^2 + 9x + 10 = 0$$
;

ii. Prove that if α and β are roots of the equation $x^2 - px - p - c = 0$ then $(1 + \alpha)(1 + \beta) = 1 - c$.

(b) Use the logarithm laws to write each of the following expression as a single logarithm:

i.
$$\log_5 x - 2$$
;

ii.
$$\frac{1}{2}\log_2 u + \frac{1}{3}\log_2 y - \frac{1}{2}[\log_2 a + \log_2 b];$$

iii.
$$2\ln(w-5) - \frac{1}{2}[\ln(x+y) - \ln(x-y)].$$

(c) Prove that

i.
$$\frac{1}{1+\sin\theta} + \frac{1}{1-\sin\theta} = 2\sec^2\theta;$$

ii.
$$\tan\left(\frac{\pi}{4} + \alpha\right) = \frac{1 + \tan\alpha}{1 - \tan\alpha}$$
.

2. (a) Differentiate the following with respect to x and simplify the answer.

i.
$$(2x+3)(5x^2-7x+1)$$
;

ii.
$$\sin(x^2 + 3)$$
;

iii.
$$e^{\cos 2x}$$

(b) Find the value of $\frac{dy}{dx}$ at the point specified:

i.
$$x^2 + y^2 = 1$$
 at $(\sqrt{2}, \sqrt{2})$;

ii.
$$x^2 + xy + y^2 = 1$$
 at $(1, -1)$;

iii.
$$x \sin y + y^2 = 1 + \frac{\pi^2}{4}$$
 at $(1, \frac{\pi}{2})$.

(c) Find the following integrals:

i.
$$\int \left(\frac{1}{3x} - \frac{3}{2x^2} + e^2 + \frac{\sqrt{x}}{2}\right) dx;$$

ii.
$$\int \left(\frac{3 + 5x - 6x^2 - 7x^3}{2x^2} \right) dx$$
;

iii.
$$\int x^3 \sqrt{x^4 + 1} \ dx$$
, you may use the substitution $t = x^4 + 1$.

