

## UNIVERSITY OF JAFFNA, SRI LANKA FACULTY OF ALLIED HEALTH SCIENCES

## FISTER YEAR FIRST SEMESTER EXAMINATION IN B.Pharm (Hons) - 2019 PHAPM 1181 PHARMACEUTICAL MATHEMATICS

Date: 27.04.2021 Time: One hour

## Answer All Questions

- 1. (a) i. If  $\alpha, \beta$  are the roots of the quadratic equation  $5x^2 6x + 3 = 0$ , form a quadratic equation whose roots are
  - $\alpha^2, \beta^2$ ;
  - $\alpha^3\beta$ ,  $\alpha\beta^3$ .
  - ii. For what values of K, the roots of the quadratic equation  $Kx^2 + 4x + (K-3) = 0$  are equal.
  - (b) Use the logarithm laws to write each of the following expression as a single logarithm:

i. 
$$\ln(a+1) - \frac{1}{3}\ln(b-1) - 3[\ln(c+2) - \ln(d-2)];$$

ii. 
$$\frac{1}{2}\log_2 u + \frac{1}{3}\log_2 y - \frac{1}{2}(\log_2 a + \log_2 b);$$

- iii.  $1 + 2\log_a b \log_a ab$ .
- (c) Prove that

i. 
$$\cos^4 \theta - \sin^4 \theta = 1 - 2\sin^2 \theta$$
;

ii. 
$$\frac{\sec x - \cos x}{1 + \cos x} = \sec x - 1.$$

(d) If  $\theta_1$  and  $\theta_2$  are acute angles such that  $\sin \theta_1 = \frac{3}{5}$  and  $\sin \theta_2 = \frac{5}{13}$ , find the numerical value of  $\sin(\theta_1 + \theta_2)$  and  $\cos(\theta_1 + \theta_2)$ . In what quadrant does the angle  $\theta_1 + \theta_2$  lie?

Continued

2. (a) Differentiate the following with respect to 
$$x$$
 and simplify the answer.

i. 
$$(3x^3 - 2x^2 + 4)(2x - 1)$$
;

ii. 
$$\frac{x^3 + 5x^2 - 2x + 4}{x^2 + 9}$$
;

iii. 
$$\sin(x^2 + 3)$$
;

iv. 
$$e^{\cos 2x}$$

(b) Find the value of 
$$\frac{dy}{dx}$$
 at the point specified:

i. 
$$x^2 + y^2 = 25$$
 at  $(3, -4)$ ;

ii. 
$$x^2 + 4xy - 2y^2 - 8 = 0$$
 at  $(0, 2)$ ;

iii. 
$$x \sin y + y^2 = 1 + \frac{\pi^2}{4}$$
 at  $\left(1, \frac{\pi}{2}\right)$ .

(c) Find the following integrals:

$$i. \int \left(3\sqrt{x} - \frac{2}{x^3} + \frac{1}{x}\right) dx;$$

ii. 
$$\int \sqrt{x}(x^2-1) dx;$$

hoseg! ]

iii. 
$$\int x^5 e^{1-x^6} dx$$
, you may use the substitution  $t = 1 - x^6$ ;

iv. 
$$\int \frac{2x \ln(x^2+1)}{x^2+1} dx$$
, you may use the substitution  $t=x^2+1$ .

## End of Exam

