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UNIVERSITY OF JAFFNA, SRI LANKA BACHELOR OF PHARMACY

Second Year First Semester Examination- 2016 PHAMM2111-Pharmaceutical Mathematics

Answer All Questions

Time Allowed: One hour

1. (a) Find the value of the discriminant and describe the nature of the roots of the following quadratic equations:

i.
$$x^2 + 12x + 32 = 0$$
;

ii.
$$-8x^2 + 5 = -4x$$
;

iii.
$$-6x^2 + 5 = -4x + 8$$
.

(b) Use the logarithm laws to write each of the following expression as a single logarithm:

i.
$$\ln(a+1) - \frac{1}{3}\ln(b-1) - 3[\ln(c+2) - \ln(d-2)];$$

ii.
$$\frac{1}{2}\log_2 u + \frac{1}{3}\log_2 y - \frac{1}{2}(\log_2 a + \log_2 b)$$
.

(c) Write down the expression for sin(A+B) and cos(A-B). Use the above expressions to find the following:

ii.
$$\cos 15^{\circ}$$
.

(d) Solve the following equations in the domain $0 \le x < 2\pi$.

i.
$$\cos^2 x - \cos x - 2 = 0$$
;

ii.
$$\sin x = \frac{1}{2}$$
.

2. (a) Find the following limits:

i.
$$\lim_{\theta \to 0} \frac{\theta^2 + 2\theta}{\sin 2\theta};$$

ii.
$$\lim_{x \to \infty} \frac{5x^3 + 1}{10x^3 - 3x^2 + 7}$$
.

(b) Differentiate the following with respect to x, simplifying your answer where possible:

i.
$$\frac{x^3 + 5x^2 - 2x + 4}{x^2 + 9};$$

ii.
$$\sin^6 x \cos^3 2x$$
;

iii.
$$(x^2 + 7x) \ln(2x^3 - 5x)$$
.

(c) By making a suitable substitution, find each of the following integrals:

i.
$$\int (5x^3 - 8)^{\frac{1}{3}}x^2 dx$$
;

ii.
$$\int (\cos(\sec x)) \sec x \tan x \, dx$$
;

iii.
$$\int \frac{x^3}{x^4 + 9} dx;$$

iv.
$$e^{\sin x} \cos x \, dx$$
.

End of Exam